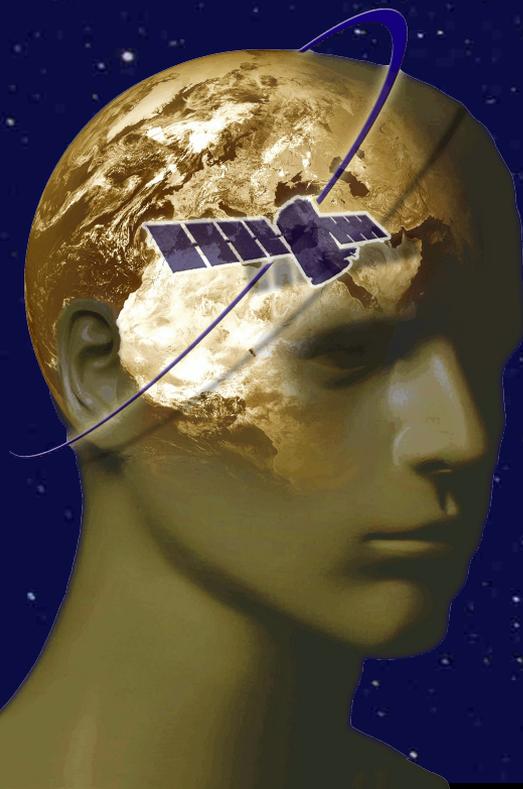
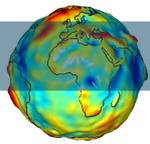


# Test of the gravitational redshift with satellites Galileo 6 and 7



**Journée GPhys**  
2015, July 6<sup>th</sup>  
Observatoire de Paris

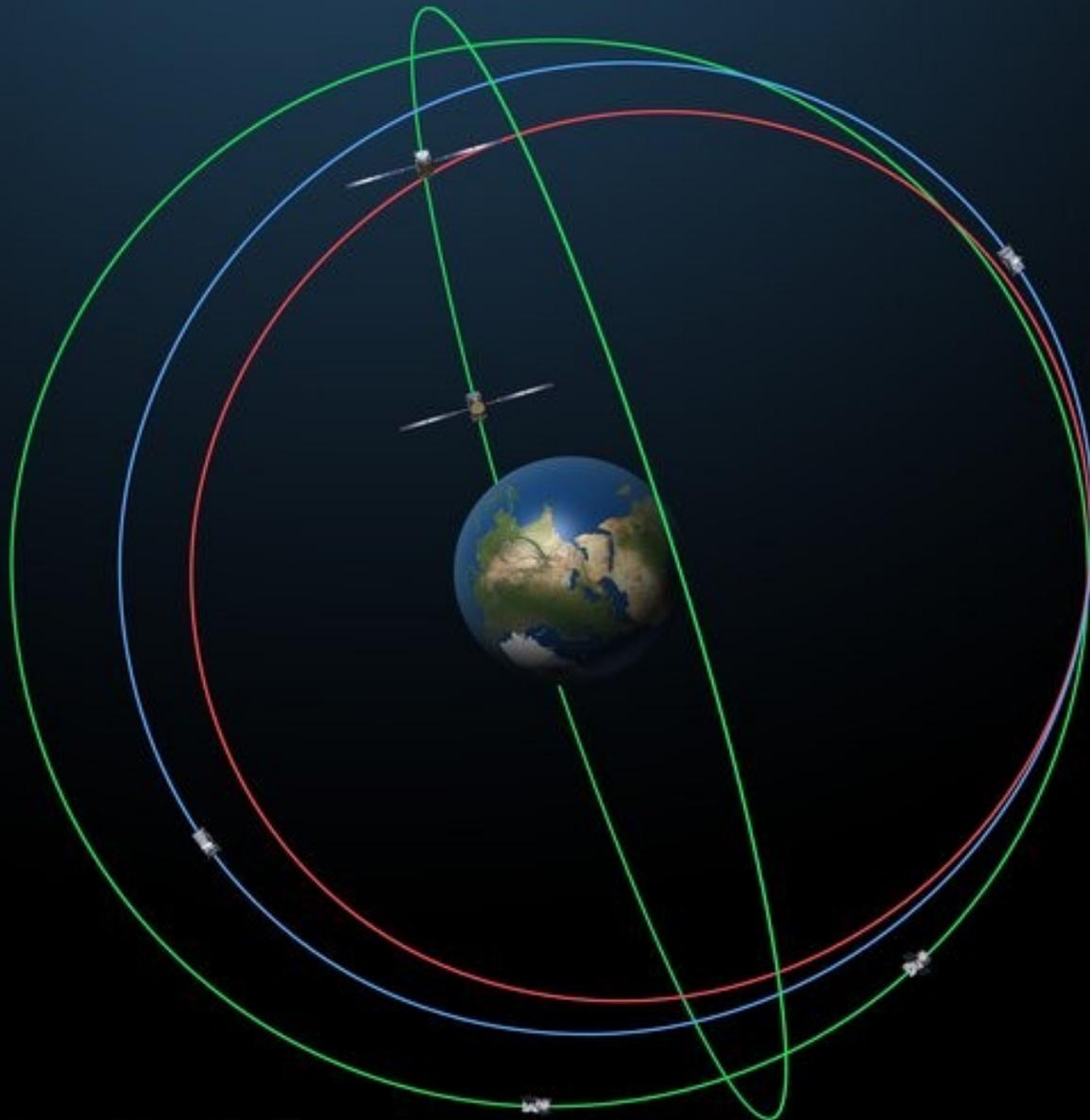
**Pacôme DELVA**  
SYRTE  
Observatoire de Paris  
Université Pierre et Marie  
Curie



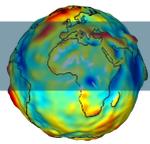
- **Galileo satellites 5 and 6** were launched with a Soyuz rocket on 22 august 2014 on the wrong orbit due to a technical problem
- Launch failure was due to a **temporary interruption of the** joint hydrazine **propellant supply** to the thrusters, caused by freezing of the hydrazine, which resulted from the proximity of hydrazine and cold helium feed lines.
- **Last launch** of Galileo satellites 7 and 8 occurred on **friday 27 march**



Navigation solutions powered by Europe



- In-Orbit Validation Galileo satellites (4)
- Uncorrected orbit of satellites 5 & 6
- Corrected orbit of satellites 5 & 6

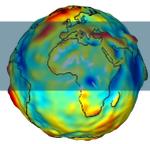


- For a Keplerian orbit one shows that :

$$\tau(t) = \underbrace{\left(1 - \frac{3Gm}{2ac^2}\right) t}_{\text{constant frequency bias}} - \underbrace{\frac{2\sqrt{Gma}}{c^2} e \sin E(t)}_{\text{eccentricity correction}} + \text{Cste}$$

constant frequency bias    eccentricity correction

- One need an **accurate clock** to measure the constant frequency bias
- The eccentricity correction is a periodic term → **use the stability of the clock to “average” the random noise**
- Limitations are due to mismodeled **systematics effects**



- RMS deviation between theory and experiment is **~ 2.2 %**
- Evidence of **systematic bias** during some particular passes

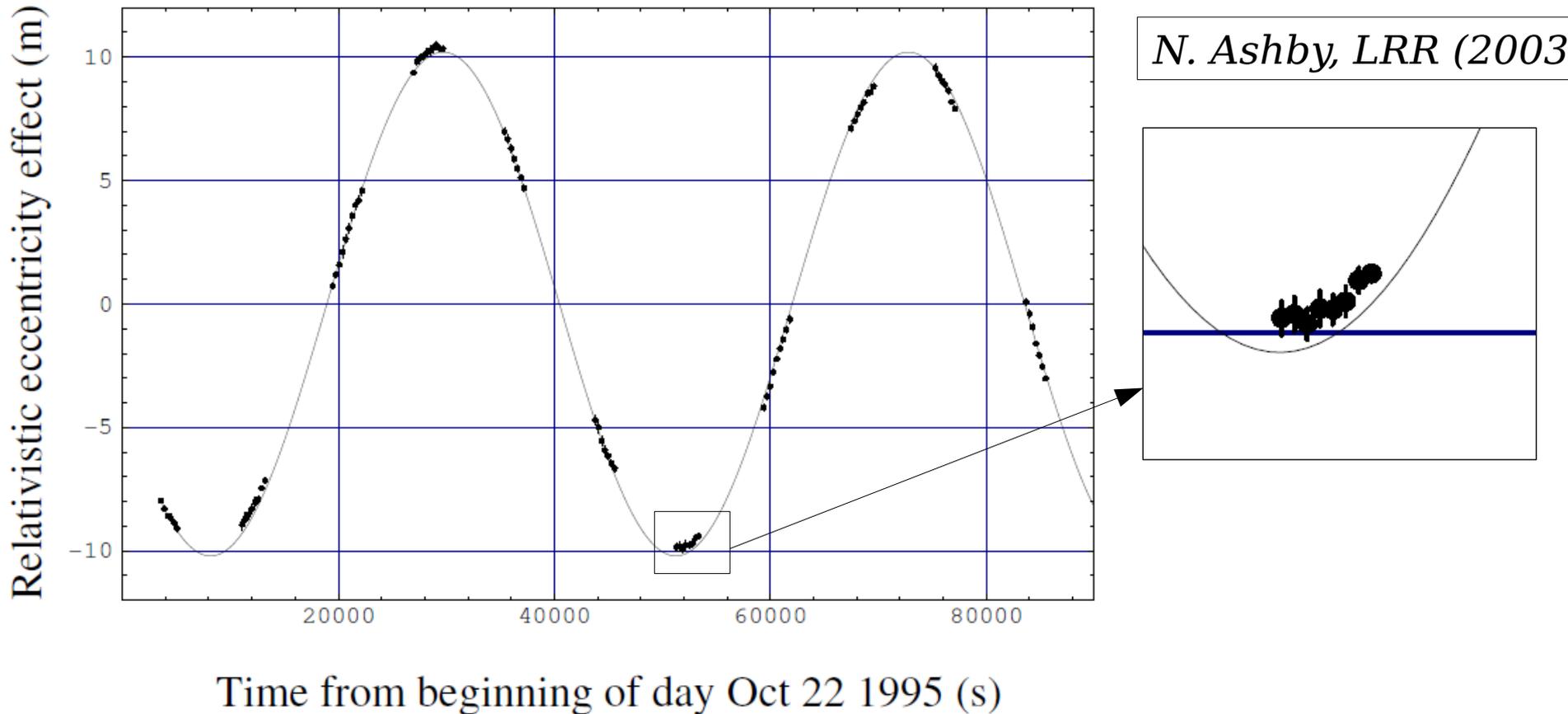
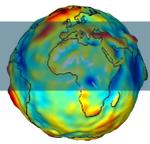


Figure 5: Comparison of predicted and measured eccentricity effect for SV nr. 13.

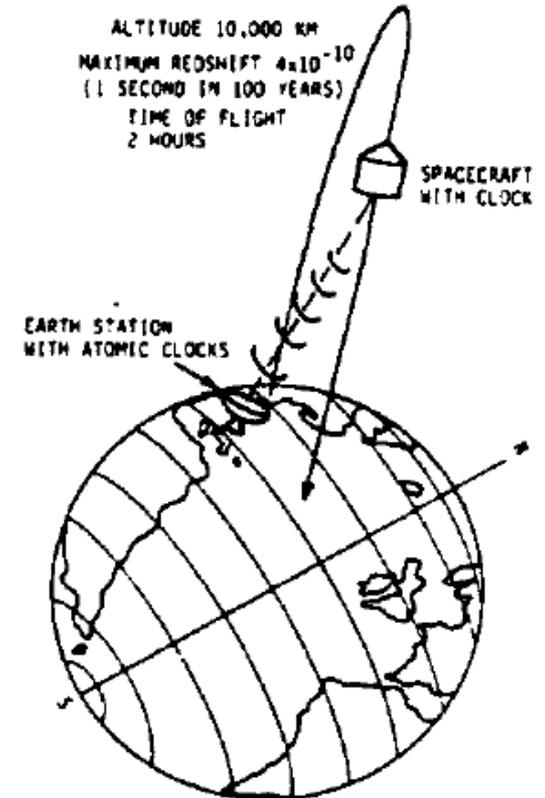
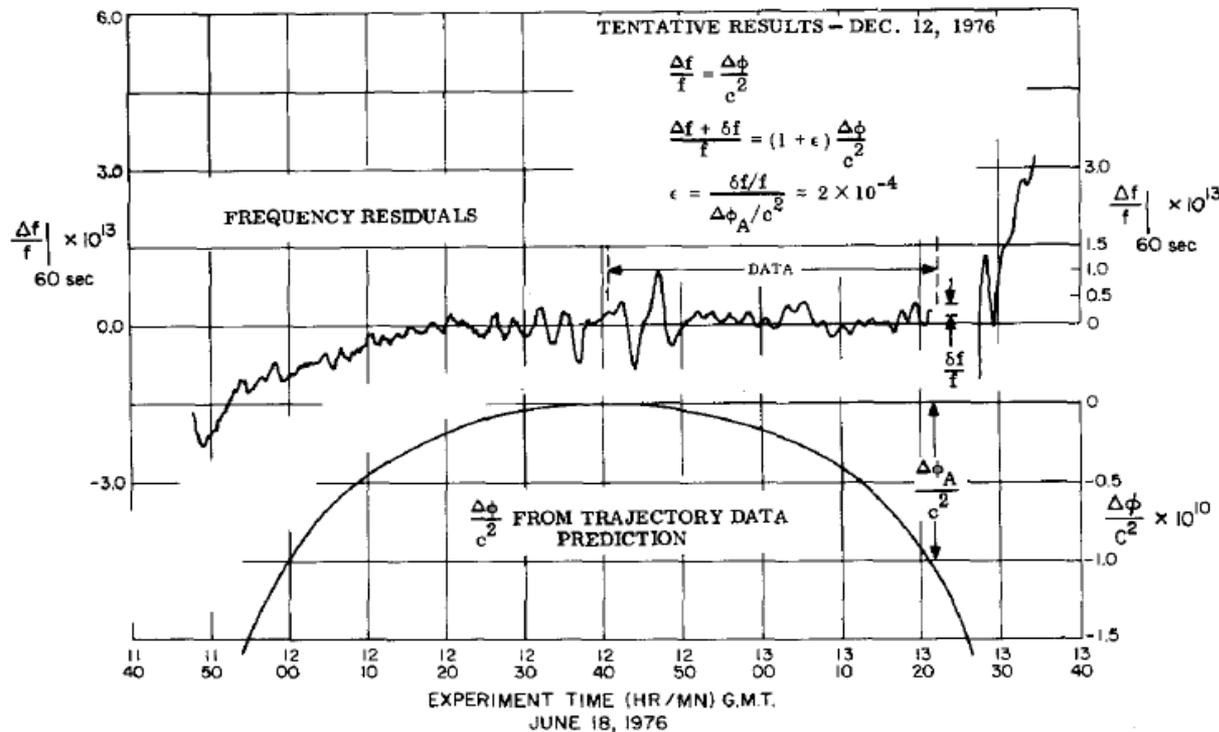


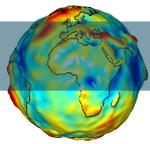
# Gravity Probe A (1976)



- Test of the redshift on a **single parabola**
- Continuous **two-way microwave link** between a spaceborne hydrogen maser clock and ground hydrogen masers
- Frequency shift verified to  $7 \cdot 10^{-5}$
- **Gravitational redshift verified to  $1.4 \cdot 10^{-4}$**

R. Vessot et al.,  
 GRG 1979, PRL  
 1980, AdSR  
 1989



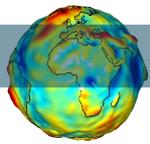


## **Simulation** of :

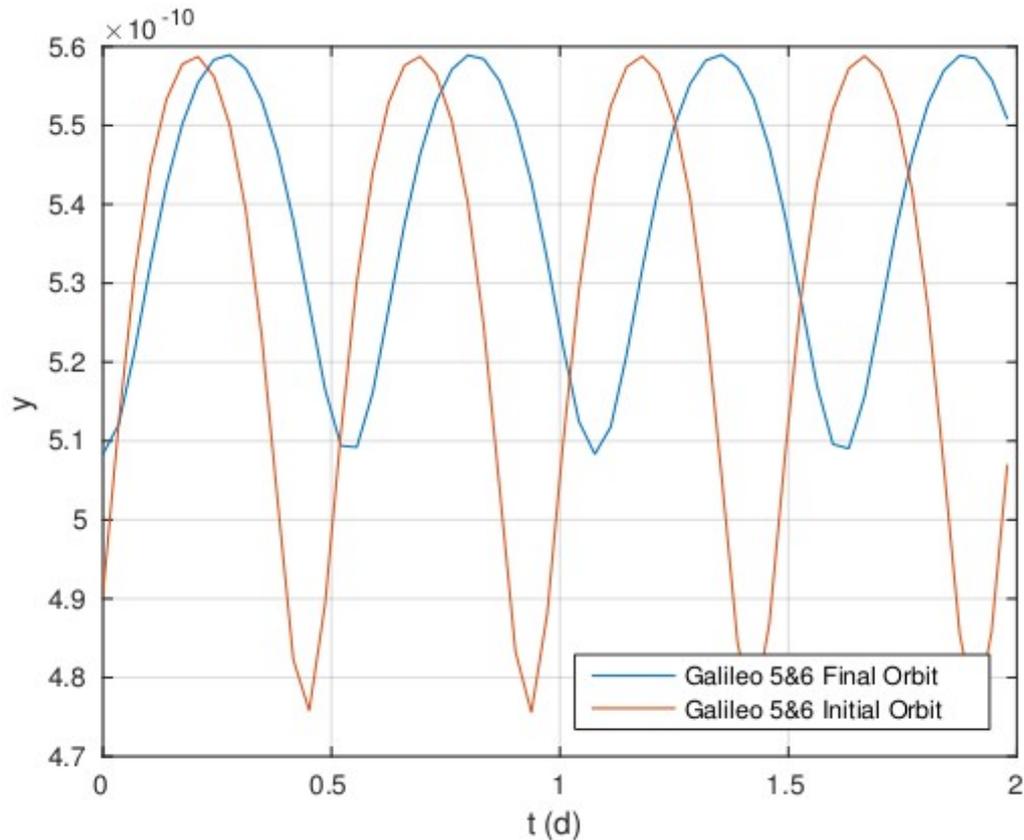
1. Galileo 5 and 6 **orbits**
2. Realistic **onboard clock noise**
3. **Gravitational Redshit Signal** (including a Local Position Invariance violation, random noise and systematic effects)

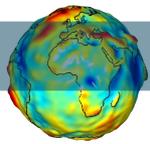
## **Analysis** of the simulated signal with two different methods :

1. **Matched Filtering** in the frequency domain
2. **Linear Least-Square + Monte-Carlo** in the time domain



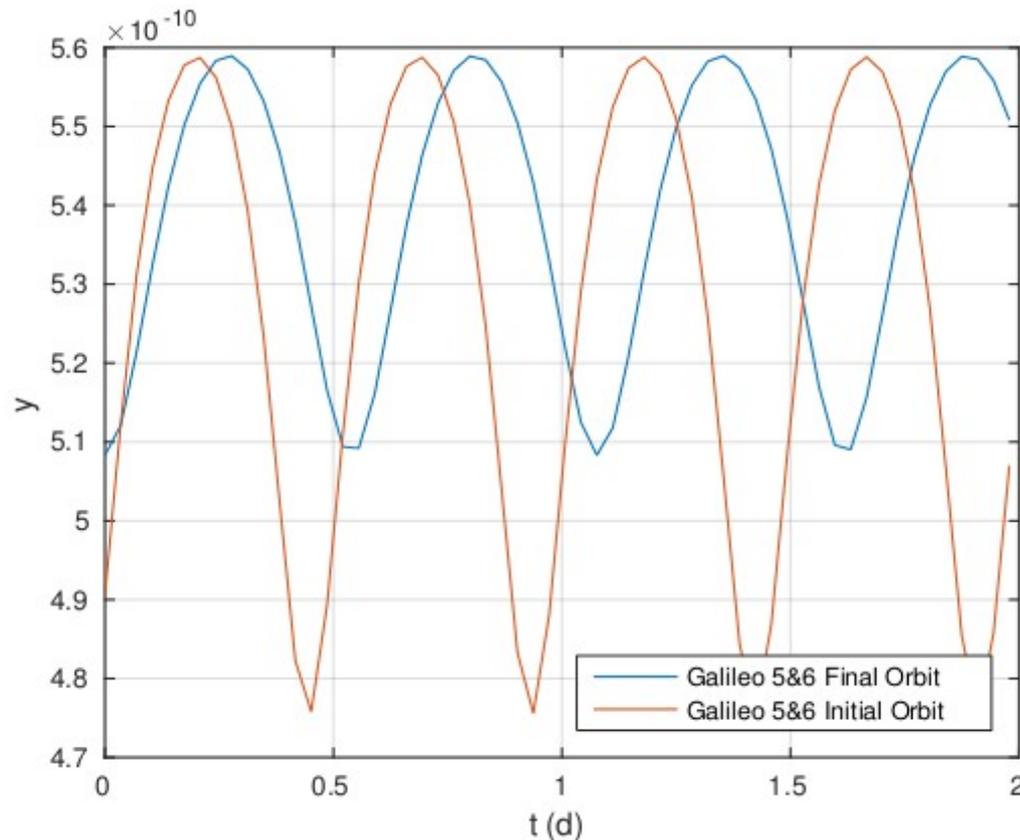
- Wrong orbit due to a technical problem : **eccentric orbit** ( $\sim 0.16$  today,  $\sim 0.23$  initially)
- Two-Lines Elements (TLE) + Kepler equation for a duration of 2 years

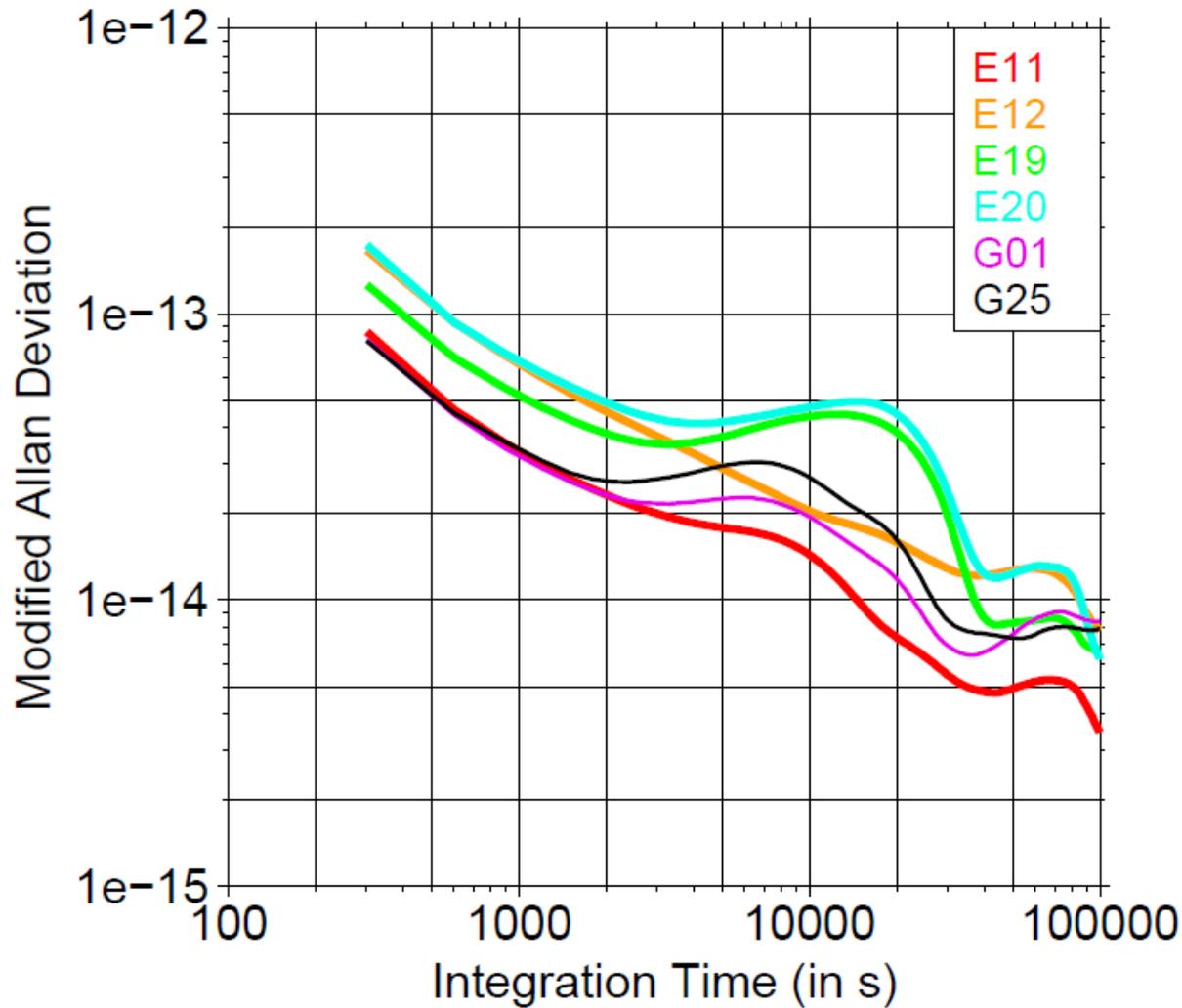
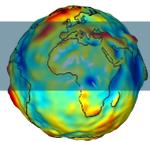




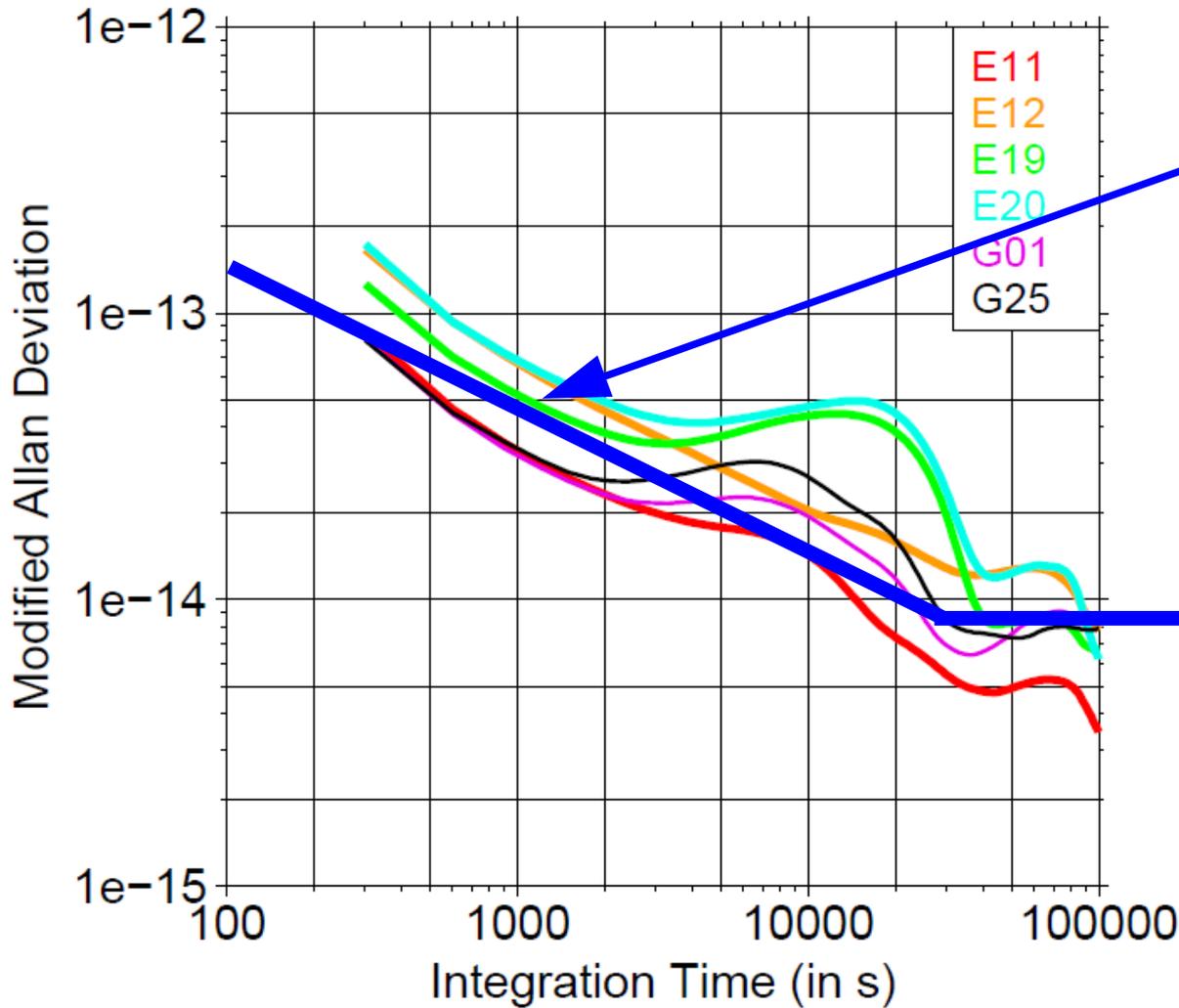
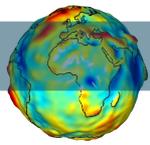
- Simple phenomenological model for LPI violation (C. Will, LRR 2014)
- Alpha is = 0 in GR
- GP-A limit :  $\alpha < 1.4 \times 10^{-4}$

$$\tilde{y}(\alpha) = -(1 + \alpha) \frac{GM}{c^2 r_s}$$





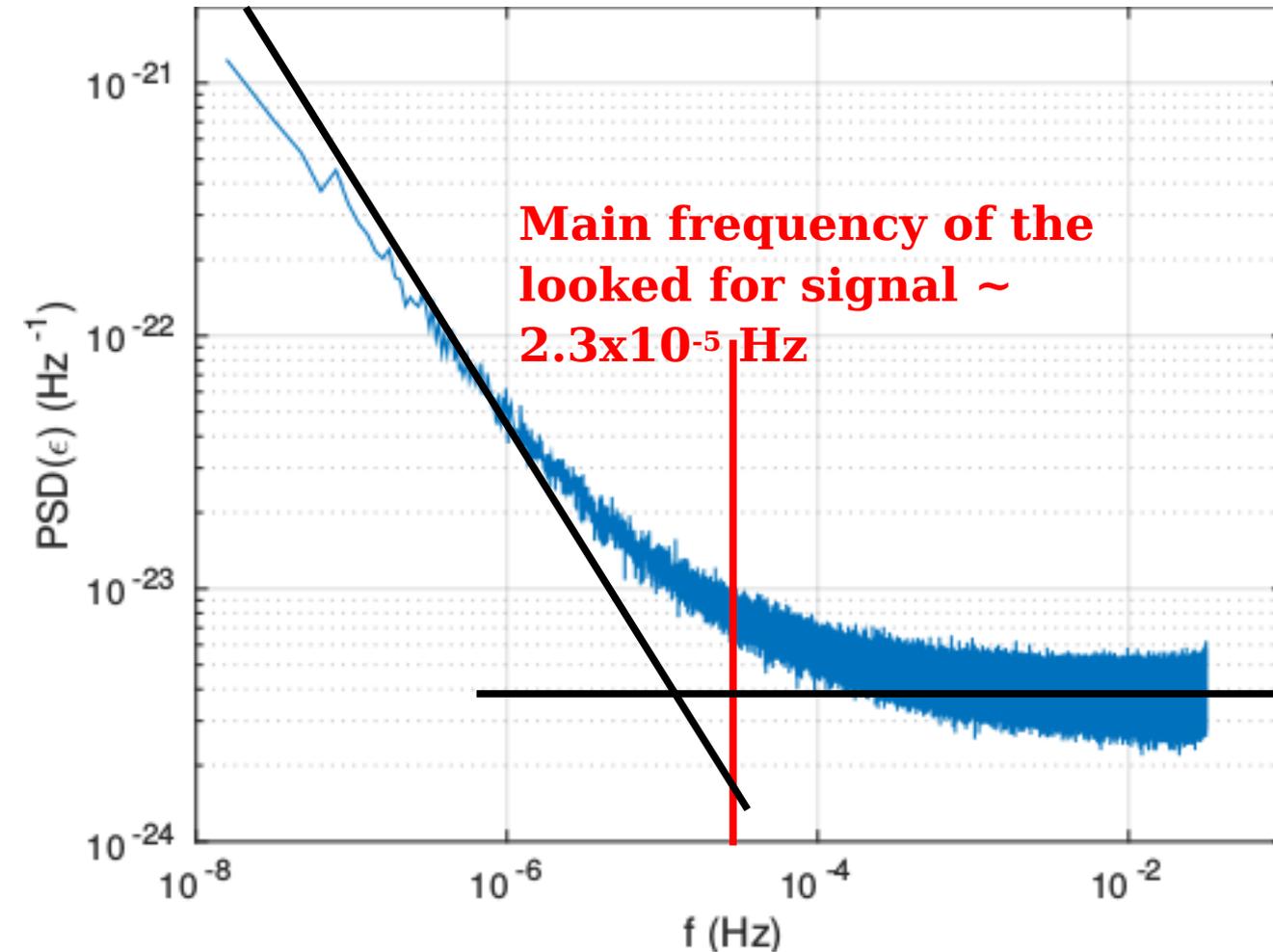
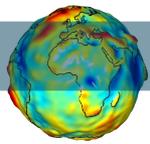
*L. Prange et al., IAG  
Potsdam  
Proceedings, 2014,  
accepted for  
publication*



## MDEV of the simulated clock noise

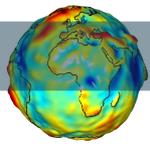
- White noise  $\sim 5 \times 10^{-14}$  @ 1000s
- Flicker noise  $\sim 8 \times 10^{-15}$

*L. Prange et al., IAG  
Potsdam  
Proceedings, 2014,  
accepted for  
publication*



## PSD of the simulated clock noise

- White noise  
 $\sim 4 \times 10^{-24}$
- Flicker noise  
 $\sim 4 \times 10^{-29}$  @ 1 Hz  
 $\sim 2 \times 10^{-24}$  @ signal frequency



### *Matched filtering method*

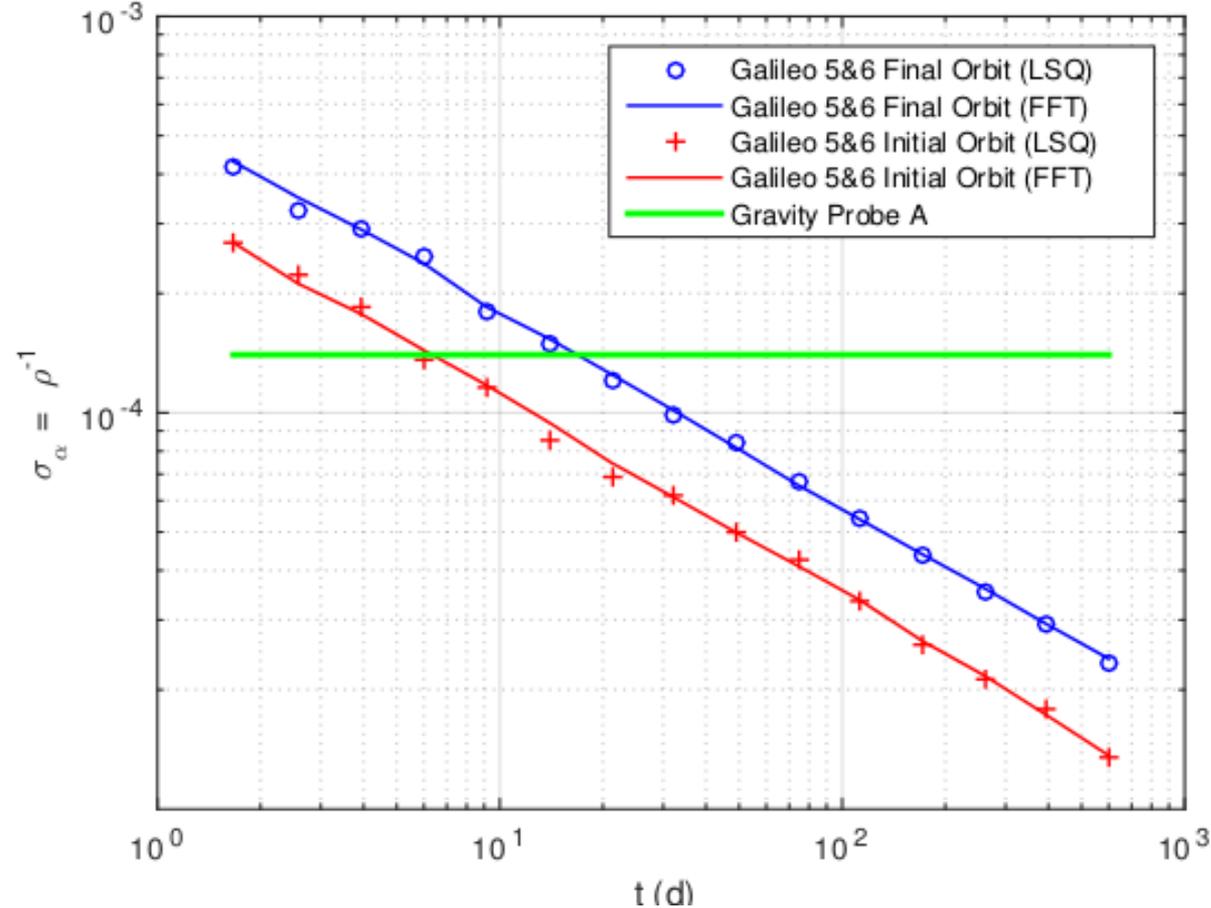
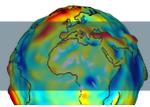
Sensitivity is the inverse of the signal-to-noise (SNR) ratio  $\rho$ , which is maximized with **matched filtering**

$$\rho^2 = \int_{-\infty}^{+\infty} \frac{|\tilde{X}(f)|^2}{S_N(f)} df \quad \left\{ \begin{array}{l} \tilde{X}(f): \text{Fourier transform of the (ideal) signal} \\ S_N(f): \text{PSD of the random noise} \end{array} \right.$$

### *Linear least-square method*

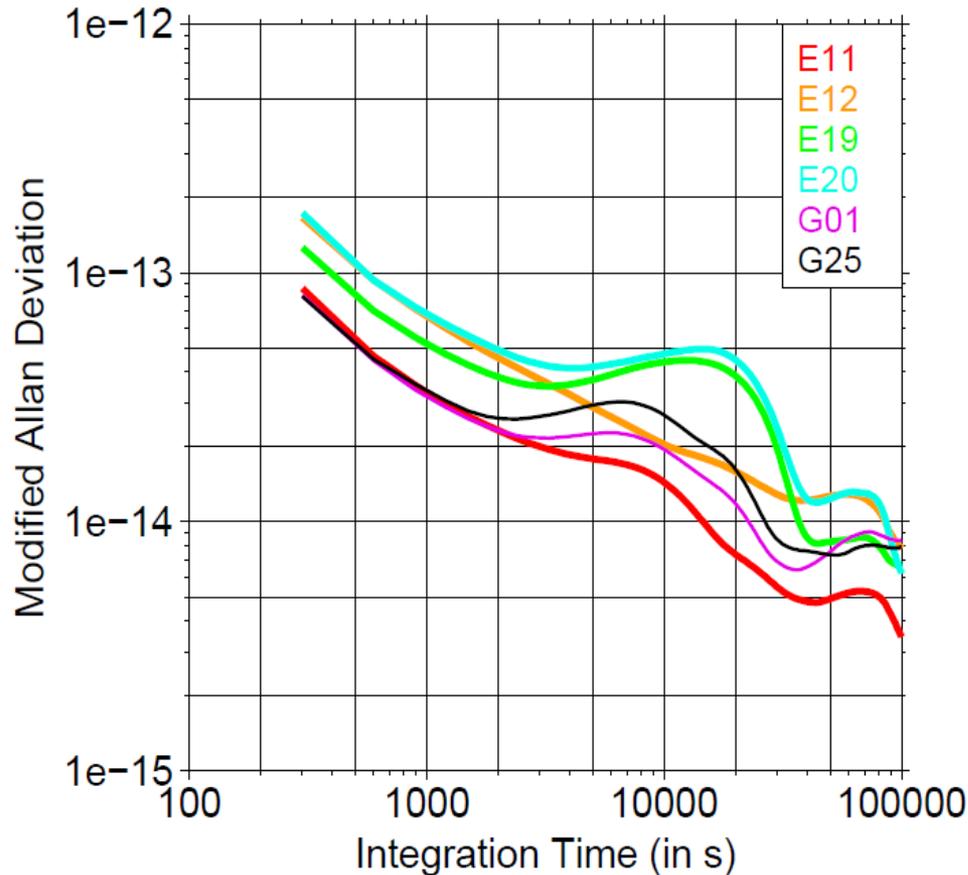
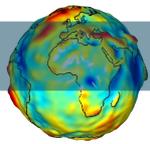
Find the minimum of the merit function  $\chi^2$  with respect to alpha

$$\chi^2 = \sum_{i=1}^N [(y(t_i) + \epsilon_i + \epsilon_{\text{sys}}) - (\tilde{y}(\alpha; t_i) + A)]^2$$



- *The best actual limit on grav. redshift (GP-A) is reached after ~2 weeks with Galileo 5*
- *After one year of integration the sensitivity is  $\sim 3 \times 10^{-5}$  → a factor of 5 better than GP-A, which was a dedicated experiment (expected sensitivity of ACES-PHARAO is 2- $3 \times 10^{-6}$ )*

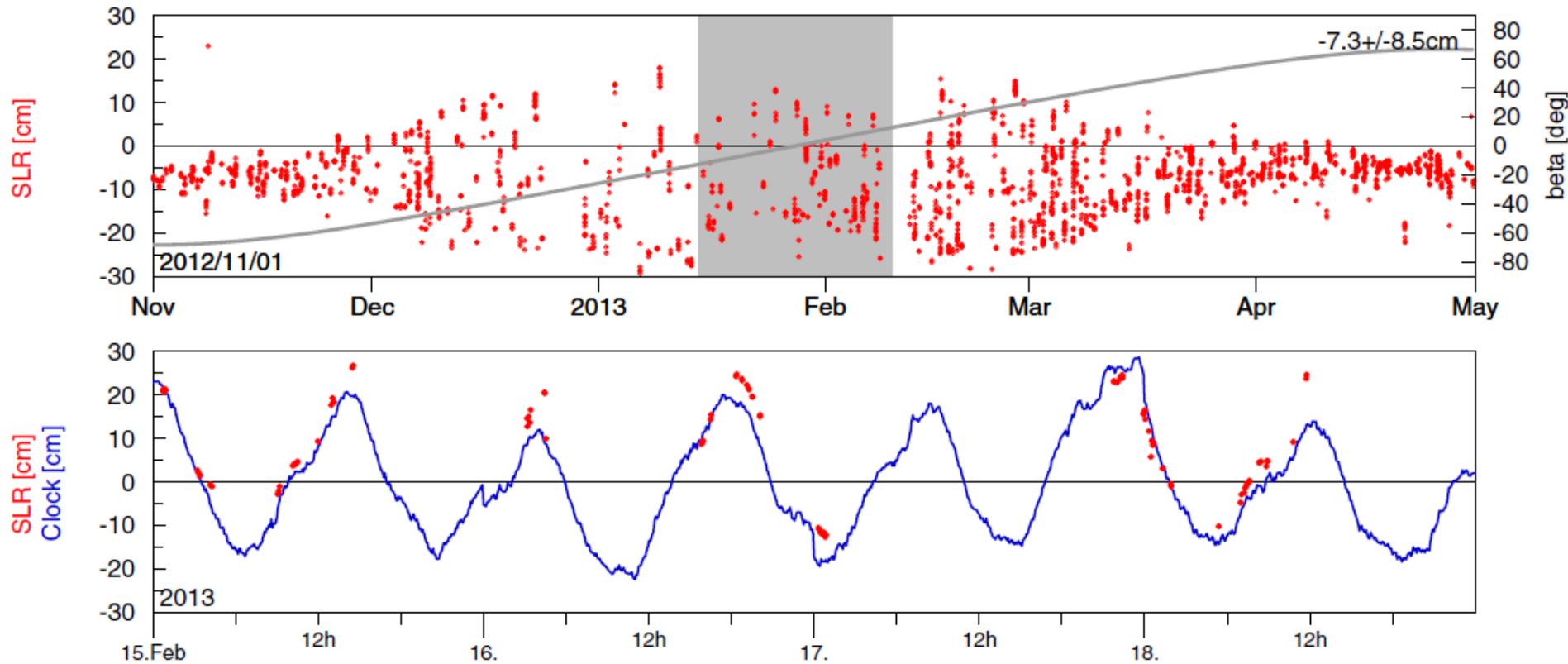
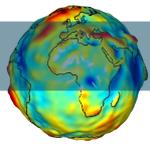
- The two very different methods agree on the sensitivity of the test
- We proved mathematically that  $\sigma_\alpha = \rho^{-1}$
- **Problem** : all systematic effects that mimic the gravitational redshift signal will induce a bias in the estimation of alpha → fake violation of LPI



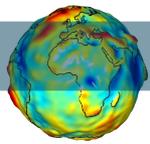
Bump in the MDEV  $\rightarrow$   
systematic effect at orbital  
frequency due to a **radial error**  
**in the estimated orbit**

(Montenbruck et al., J.Geo.,  
2014)

$\rightarrow$  mimick a grav. redshift  
violation !

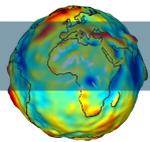


- Systematic effect shows a **dependency with the sun elevation angle**, ie. the direction of Sun w.r.t. the satellite orbital plane (Montenbruck et al., J.Geo., 2014)
- At least 75 % of this effect due to **mismodeling of Solar Radiation Pressure** (SRP), other effects could be due onboard temperature variations

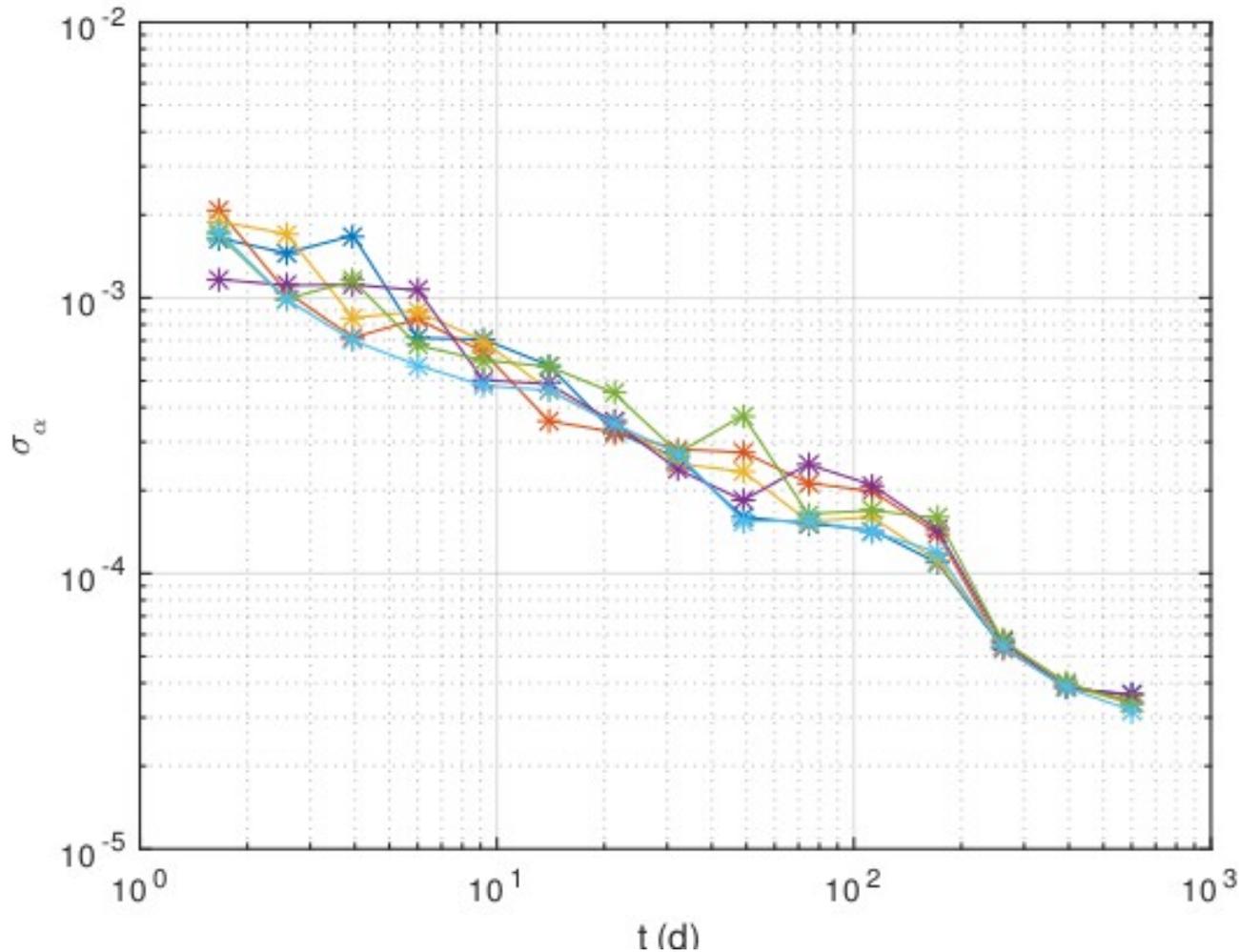


- Systematic effect due to mismodelling of the SRP :
  - Effect at orbital frequency with a frequency shift (1/year) (linked to the direction of the Sun)
  - Amplitude modulation at frequency (1/year)

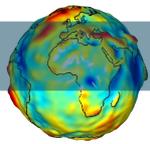
$$\epsilon_{\text{sys}} = A \sin((n_{\text{sat}} + \omega_{\text{year}})t + \phi_1)(1 + B(\cos(\omega_{\text{year}}t + \phi_2) - 1)), \quad \omega_{\text{year}} = 2\pi/\text{year}$$



$$\epsilon_{\text{sys}} = A \sin((n_{\text{sat}} + \omega_{\text{year}})t + \phi_1)(1 + B(\cos(\omega_{\text{year}}t + \phi_2) - 1)), \quad \omega_{\text{year}} = 2\pi/\text{year}$$



**Decorrelation  
between fit  
parameters occurs  
for 1 year  
integration time**



- it will be possible, with Galileo satellites 5 and 6, and at least one year of data, to improve on the GP-A (1976) limit on the gravitational redshift test, down to an accuracy around  $3\text{-}5 \times 10^{-5}$
- Detailed study of random and systematics effects (article submitted)