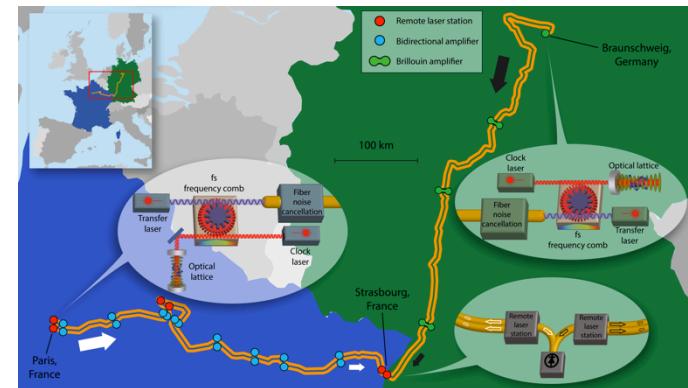
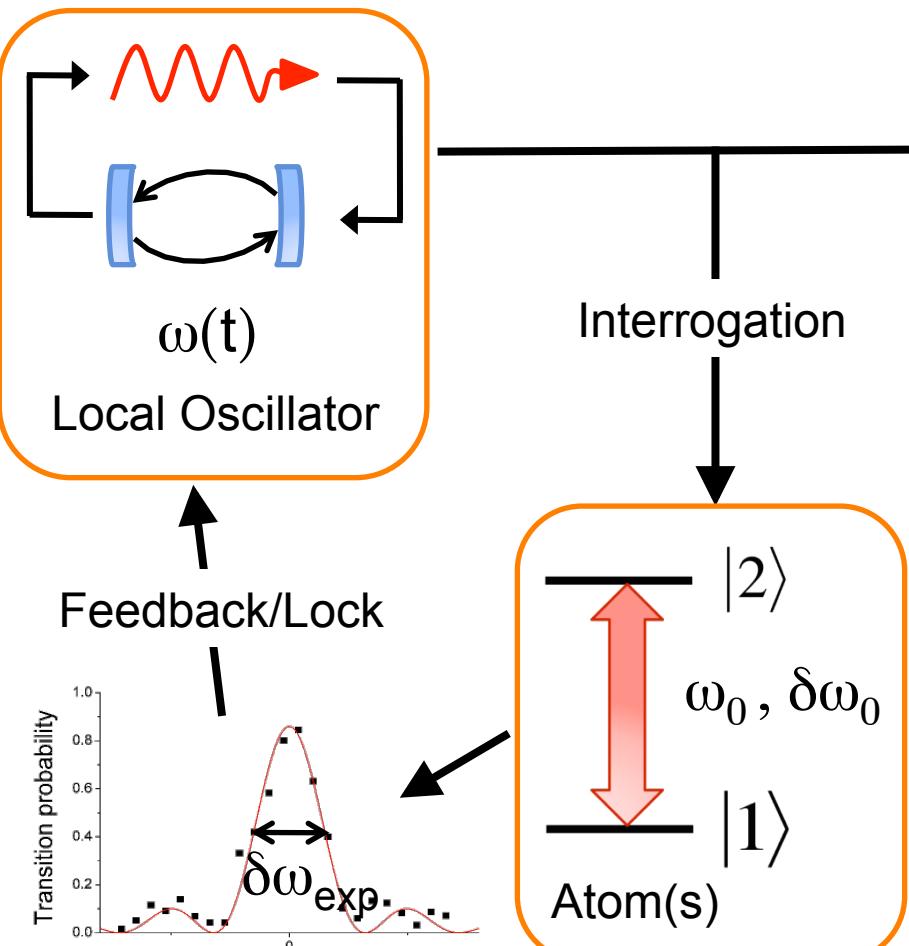


# STRONTIUM OPTICAL LATTICE CLOCKS

Eva Bookjans  
GPHYS, July 6<sup>th</sup> 2016



# ATOMIC CLOCKS



Transition probability  
detection

$$\text{Frequency Reference} \\ \omega(t) = \omega_0(1+\varepsilon+y(t))$$

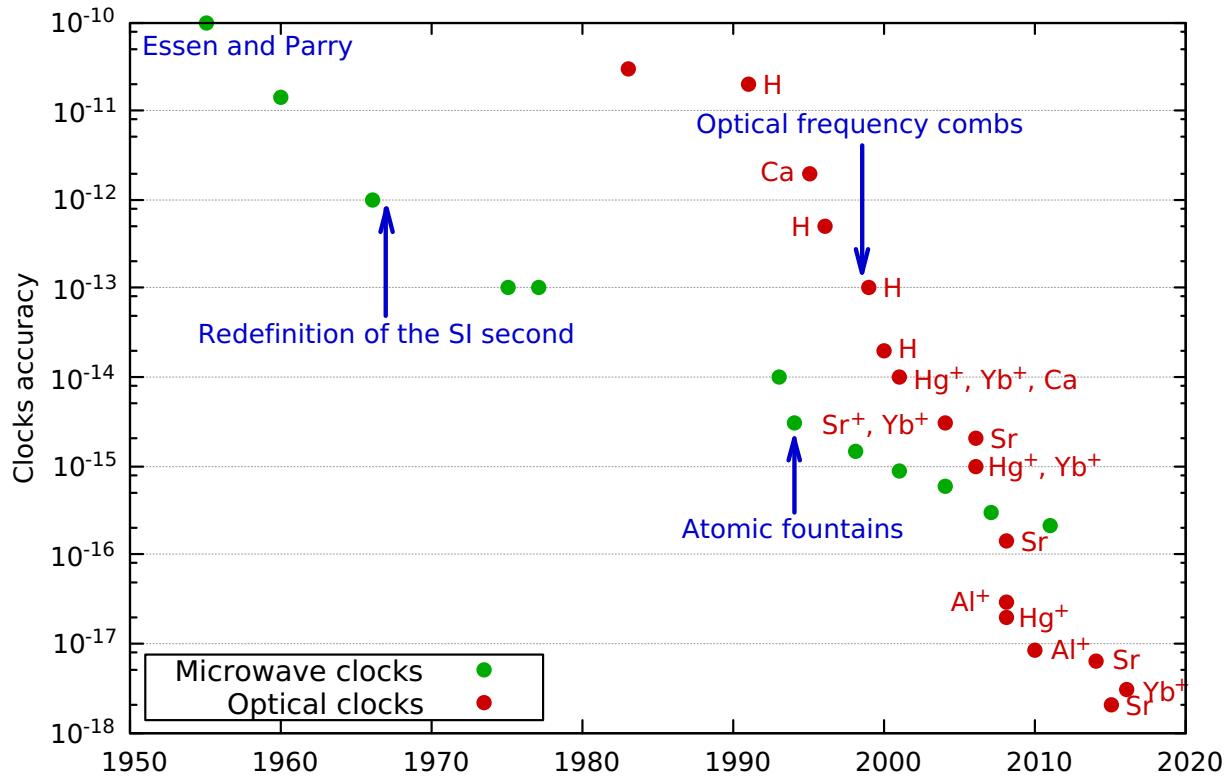
- $\varepsilon$  – systematic frequency shifts
- $y(t)$  – frequency noise



- fractional stability:  
$$\sigma_y(\tau) \sim \frac{1}{Q(S/N)} \tau^{-1/2}$$
- atomic quality factor:

$$Q = \omega_0 / \delta\omega$$

# HISTORY OF ATOMIC CLOCK ACCURACY



○ Microwave clocks:

$$\omega_0/2\pi \approx 10^{10} \text{ Hz}$$

$$\Rightarrow Q \approx 10^{10}$$

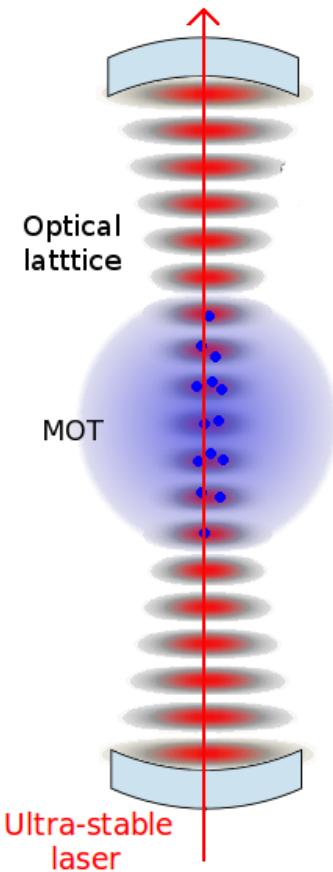
○ Optical clocks:

$$\omega_0/2\pi \approx 10^{15} \text{ Hz}$$

$$\Rightarrow Q \approx 10^{15}$$

- Optical clocks improve both the accuracy and the frequency stability

# OPTICAL LATTICE CLOCKS



- Probe on a narrow optical resonance with an ultra-stable “clock” laser (**high Q**)
- Trap atoms in an optical lattice potential
  - Lamb-Dicke regime: **insensitive to motional effects**
  - trap light at magic wavelength: minimal light-shift effects
  - Large number of interrogated atoms (unlike with ion traps): **high SNR**
- Record stability: a few  $10^{-16} / \tau^{1/2}$
- Record accuracy: a few  $10^{-18}$



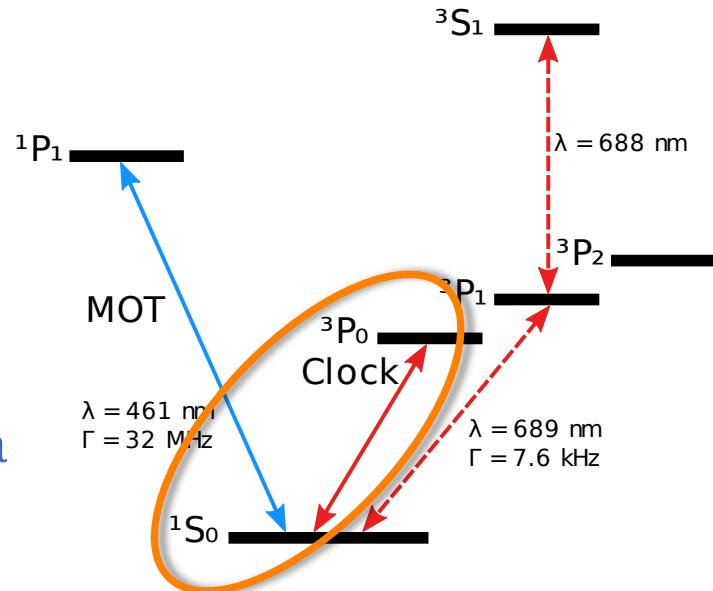
# DIFFERENT OPTICAL LATTICE CLOCK SPECIES AT LNE-SYRTE

## ○ Sr lattice clock

- required laser sources are accessible with semi-conductor technology: **transportable clocks**
- implemented in many laboratories: good candidate for a new **SI second**

## ○ Hg lattice clock

- requires UV lasers: **technically challenging**
- low sensitivity to BBR: **excellent ultimate accuracy**



# TWO STRONTIUM OPTICAL LATTICE CLOCKS



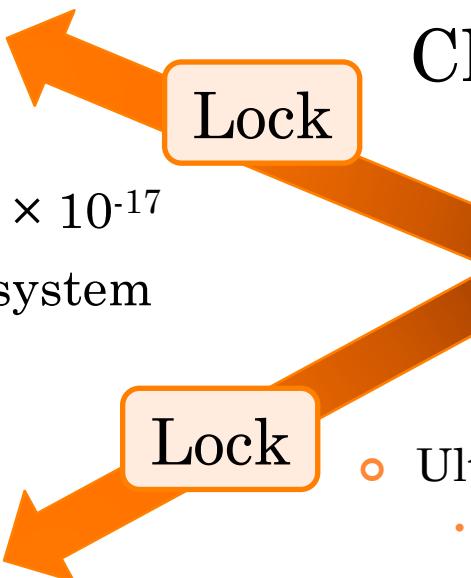
Sr1

- Accuracy :  $4\text{-}5 \times 10^{-17}$
- New vacuum system



Sr2

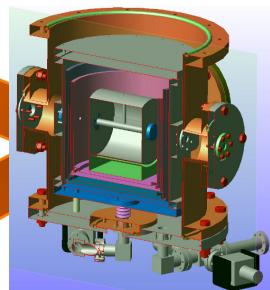
- Accuracy :  $4.1 \times 10^{-17}$
- Operational measurements



Clock laser

- Ultra-stable cavity
  - 10 cm ULE spacer and silica mirrors
  - thermal shielding
- Residual drift of a few 10s of mHz/s

Optical frequency comb



Comparisons  
with other  
clocks



# ACCURACY BUDGET (SR2)

Main contributions in  $10^{-18}$ :

Effect	Correction	Uncertainty
Blackbody radiation shift	5208	20
Quadratic Zeeman shift	1317	12
Lattice light shift	-30	20
Lattice spectrum	0	1
Density shift	0	8
Line pulling	0	20
Probe light-shift	0.4	0.4
AOM phase chirp	-8	8
Servo error	0	3
Static charges	0	1.5
Blackbody radiation oven	0	10
Background collisions	0	8
<b>Total</b>	<b>6487.4</b>	<b>41</b>

Remains the most important contribution

Otherwise limited by statistics

## OTHER GROUPS

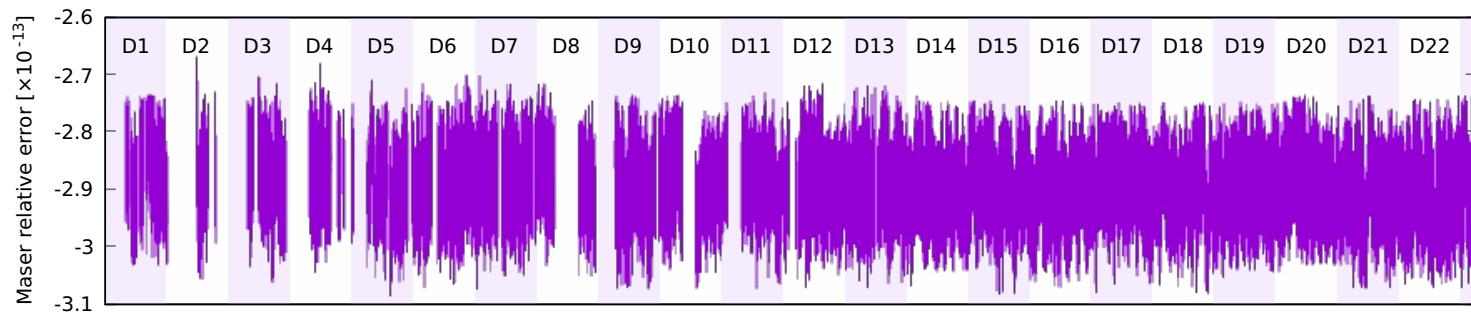
- JILA: Sr optical lattice clock with  $2 \times 10^{-18}$  accuracy
- NIST: Stability down to  $1.6 \times 10^{-18}$  after 7h of integration between two Yb clocks
- PTB: Sr optical lattice clock with  $1.9 \times 10^{-17}$  accuracy and an ultra-stable laser with a  $8 \times 10^{-17}$  noise floor
- Riken: Comparison between two cryogenic Sr clocks with  $7.2 \times 10^{-18}$  accuracy
- NPL (Sr), NMIJ (Sr,Yb), NICT (Sr), NMI (Sr),...



# OPERATIONAL OPTICAL CLOCKS

- Improvement of **statistical resolution**
  - allow for characterization of systematic effects
- **Clock comparisons**
- Space clocks, e.g. **Pharao/ACES space mission**
- Establishment of time scales with optical clocks
  
- **Goal:** reach a level of maturity equivalent to the Cs based clock architecture

Jun. 2015: Unattended operation of 31 days, 83% uptime (ITOC JRP)



# CLOCK COMPARISONS

- Test the **reproducibility** of optical lattice clocks
- Creation of a network of optical lattice clocks
  - eventual establishment of **time scales** with optical clocks
- Determine and track **frequency ratios** between different atomic species
  - probe of fundamental physics
- Measure offsets and variations of the **geo-potential**
  - applications in geophysics



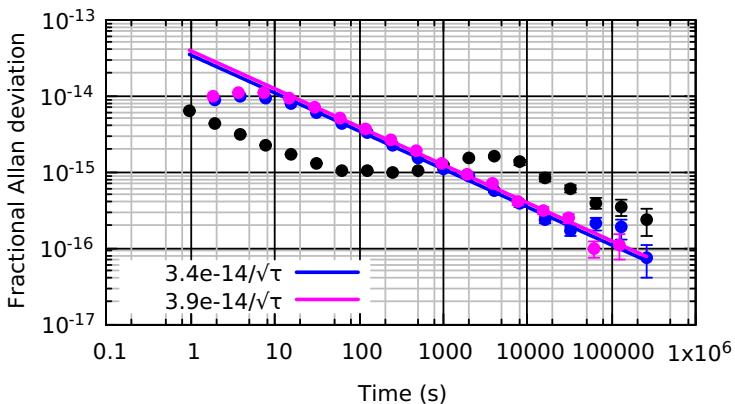
# MEANS OF COMPARISON

- Local/on-site comparisons
  - through shared LOs (e.g. clock laser), fiber links, cables
- Stabilized optical **fiber links**
  - allows for direct optical-to-optical frequency comparisons
  - limited to intercontinental scales
- **Satellite links (GPS/TWSFTF )**
  - allows worldwide comparisons of clocks
  - limited resolution (sufficient for microwave clocks but not for optical clocks)
- **Pharao/ACES space clock** on board the ISS (2018)
  - time limited mission (3-5 years?)



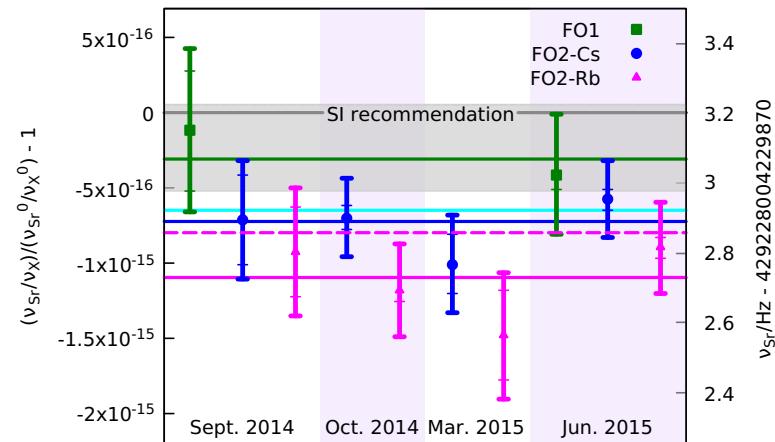
# LOCAL COMPARISONS AT LNE-SYRTE SR CLOCK VS. MICROWAVE CLOCKS

## Stability



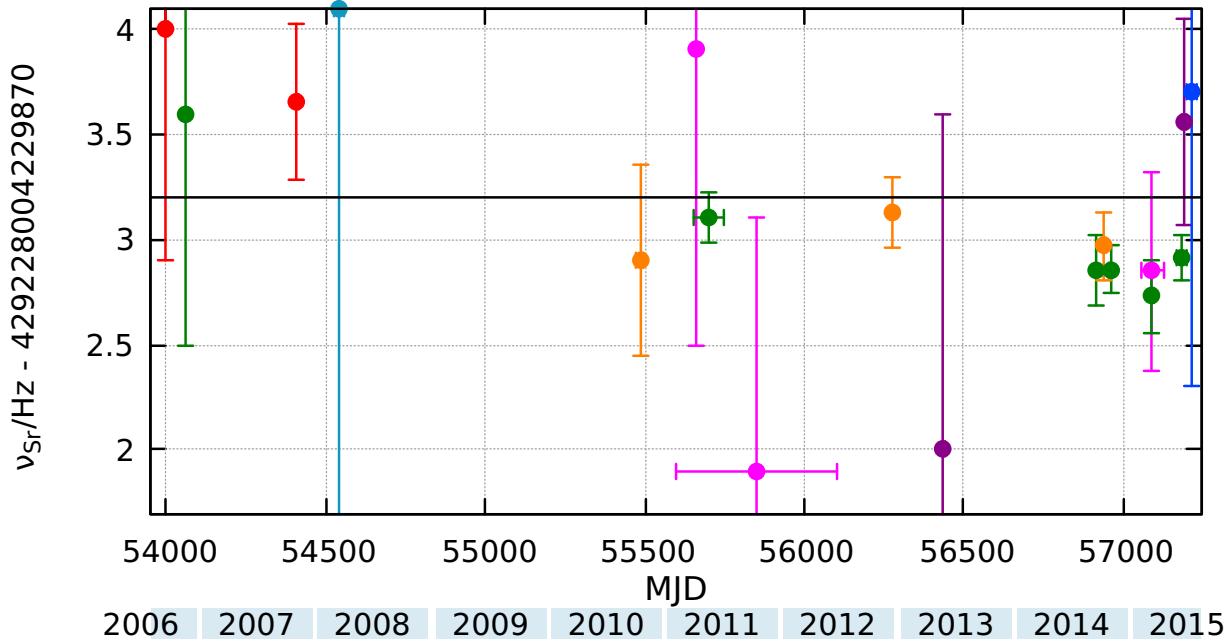
- limited by QPN of the microwave fountains
- $10^{-16}$  resolution after 12h
- mid  $10^{-17}$  resolution after 7 days

## Accuracy



- limited by accuracy of the fountains
- international agreement

# ABSOLUTE FREQUENCY OF THE SR CLOCK TRANSITION



- SYRTE, PTB, JILA, Tokyo University, NICT, NMIJ, NIM
- Track potential variations of fundamental constants:

$$\frac{d \ln(v_{Sr}/v_{Cs})}{dt} = -1.6 \times 10^{-16} \pm 6.5 \times 10^{-17} / \text{year}$$

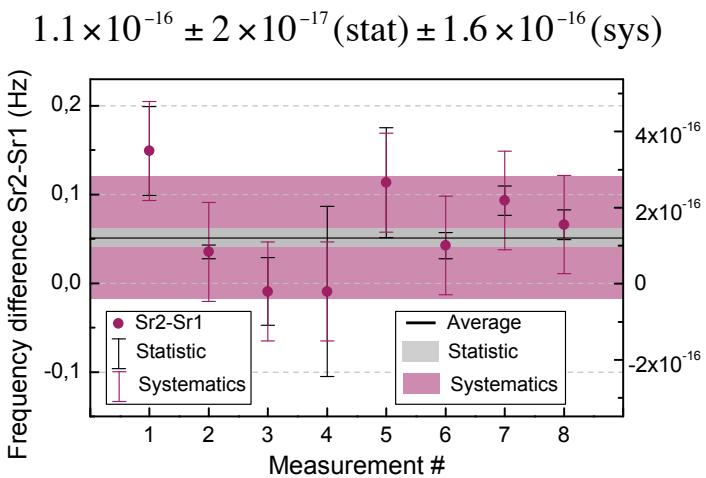
Annual variation of  $v_{Sr}/v_{Cs}$  with relative amplitude:  $5.5 \times 10^{-17} \pm 1.8 \times 10^{-16}$



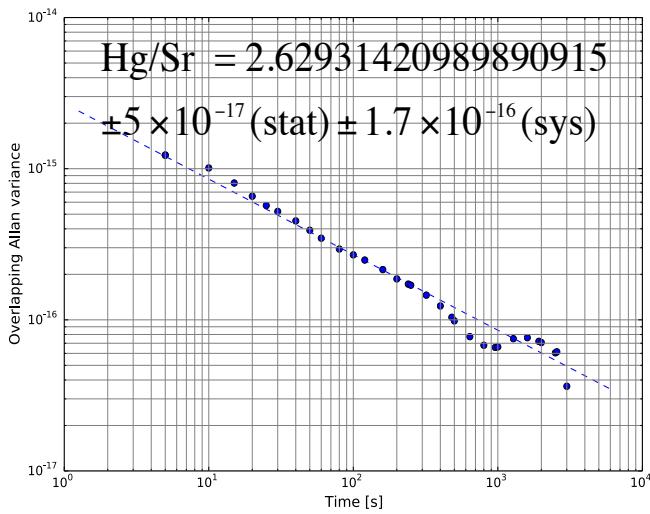
# LOCAL COMPARISONS AT LNE-SYRTE

## OPTICAL VS. OPTICAL

### ○ Sr vs. Sr



### ○ Sr vs. Hg



- First agreement between OLCs
- Detection and characterization of several systematic effects

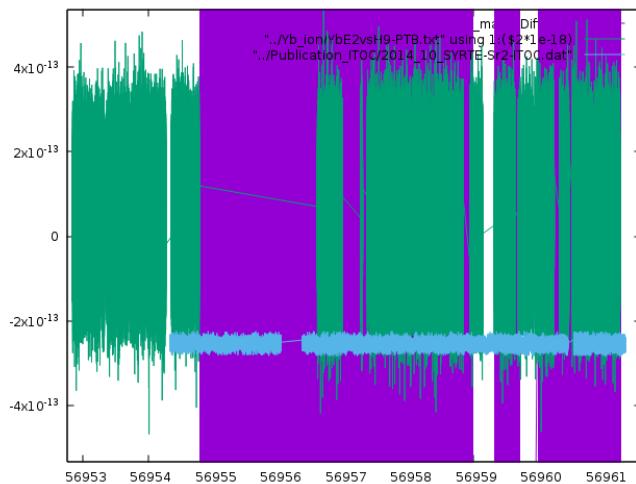
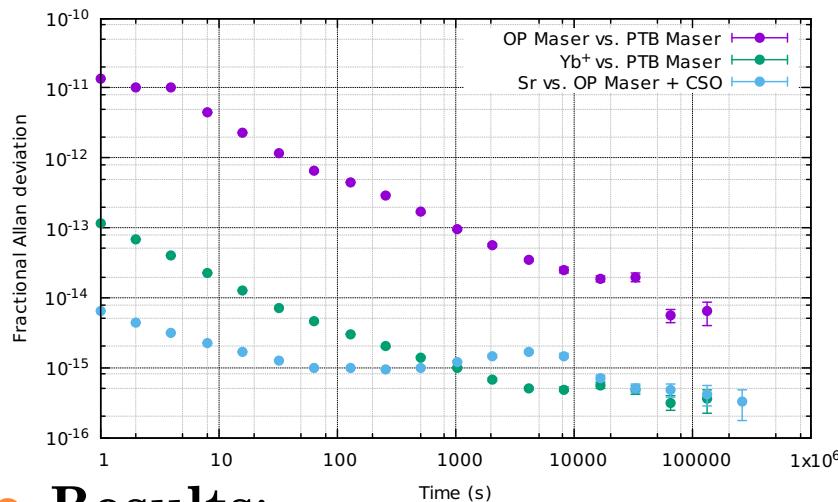
R. Le Targat *et al.*, Nat. Commun. (2013)

- Direct optical-to-optical frequency measurement (via fiber comb)
- Best reproduced frequency ratio (with RIKEN, Tokyo)

R. Tyumenev *et al.*, arXiv:1603.02026

# INTERNATIONAL CLOCK COMPARISONS VIA TWSTFT

- Comparison of Sr vs. Yb+ (PTB, NPL) via TWSTFT (ITOC JRP project)



## Results:

- Statistical resolution only in the mid  $10^{-16}$  even after 7 days of measurements
  - limited by the link
- Frequency ratio compatible with independent local measurements
- 3 weeks comparison achieved in June 2015 with many more clocks!

# INTERNATIONAL CLOCK COMPARISONS VIA FIBER LINKS

- **Goal: high resolution comparison:**

- Direct comparison of optical clocks over a **continental scale**
- Pure optical comparison, not limited by
  - Microwave transfer methods
  - Microwave oscillators
- Preservation of the frequency stability over long distances

- **Implementation:**

- Disseminate an IR (1542 nm) “vector” narrow laser through **phase-compensated optical fibers**
- **Optical frequency combs** to measure  $v_{\text{IR}}/v_{\text{clock}}$  on both sides

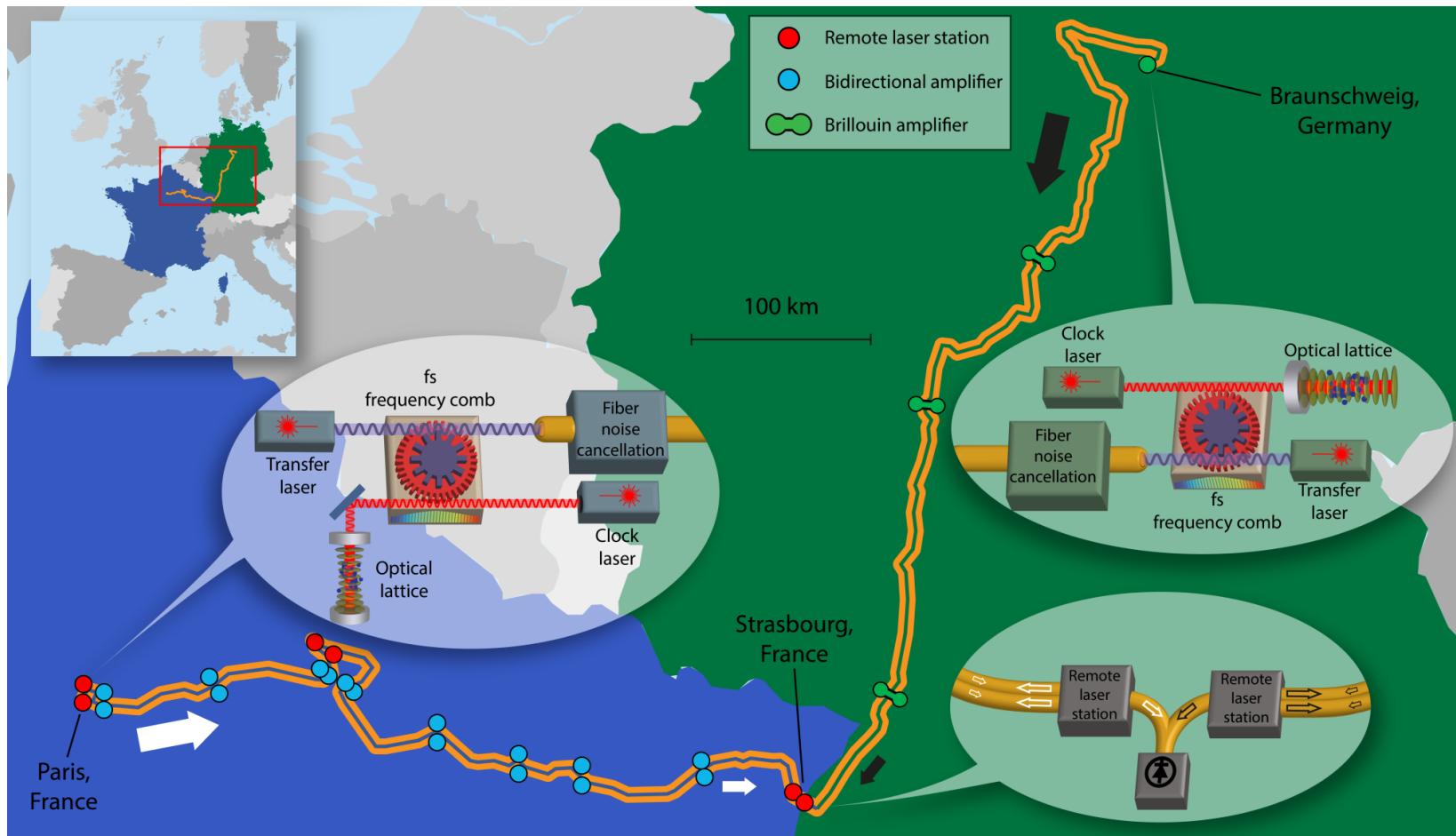
- **Challenges:**

- Fiber **attenuation** (e.g. 450 dB for 1500 km) – need amplifiers
- **Availability** of fibers (dark channel or dark fibers)
- Propagation **delays** (cascaded links)
- **Power limits** (non-linear effects, disturbance of telecom networks)



# SYRTE – PTB LINK VIA LPL

PTB, LPL and SYRTE established a 1415 km long optical fiber link and performed in 2015 the **first direct comparison of optical clocks** on a continental scale.

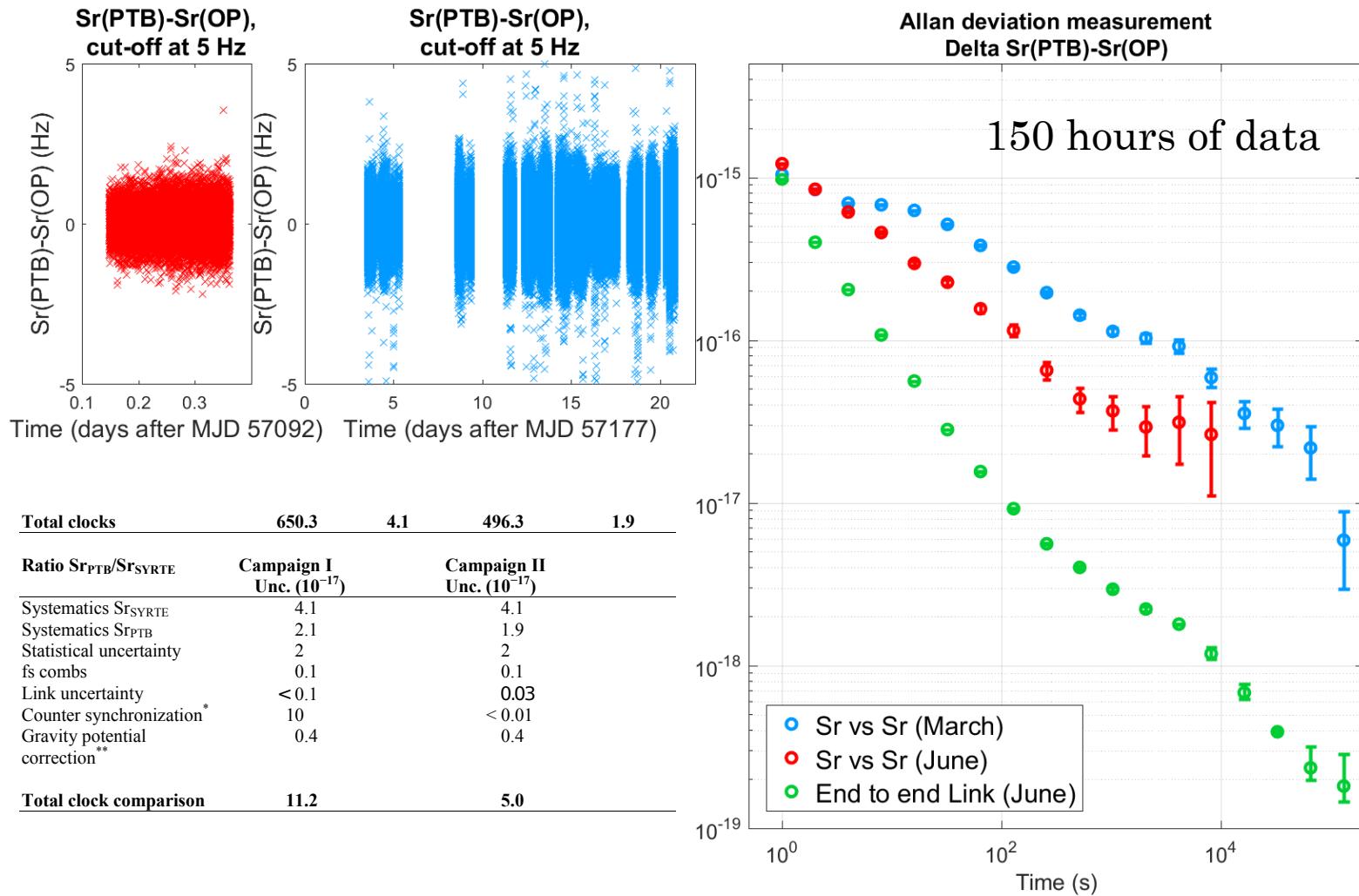


# COMPARISON OF TWO REMOTE AND COMPLETELY INDEPENDENT CLOCKS

	PTB	SYRTE
Loading of the atoms	Blue MOT-Red MOT	Blue+atomic drain
Lattice light	TiSa pumped by a multimode pump	TiSa pumped by a monomode pump
BBR Shield from oven	No direct line of sight	Deflected atomic beam
Lattice orientation	Horizontal	Vertical
Lattice effect	Retroreflected light	Cavity-formed + PDH lock
Clock laser	48 cm long cavity, flickering at $8 \times 10^{-17}$	10 cm long cavity, flickering at $5 \times 10^{-16}$
Density of atoms	1-2 atoms/site	5-10 atoms/site
Coils	In-vacuum MOT coils	MOT coils outside of vacuum
Gravitational redshift	$-247.4 (\pm 0.4) \times 10^{-17}$	
Uncertainty budgets	$1.9 \times 10^{-17}$	$4.1 \times 10^{-17}$

- Only agreement between completely independent optical clocks
- Second to best comparison of optical lattice clocks

# 2 MEASUREMENT CAMPAIGNS



Statistical uncertainty:  $2 \times 10^{-17}$  after 1 hour

$\text{SrPTB}/\text{SrSYRTE} - 1 = (4.7 \pm 5.0) \times 10^{-17}$  C. Lisdat *et al.*, Nat. Commun. (2016)

# APPLICATIONS:

- **Gravitation:**

- Correction for the **gravitational redshift**:
  - $(-247.4 \pm 0.4) \times 10^{-17}$  corresponding to a 4 cm uncertainty of the (geodetic) height of the clocks
- The next generation of remote clocks comparison will improve our knowledge of the gravitational potential of the Earth

- **Fundamental Sciences:**

- Precise measurement of **frequency ratios**
- Search for variation of **fundamental constants**, detection of dark matter



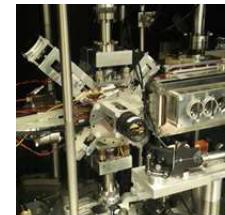
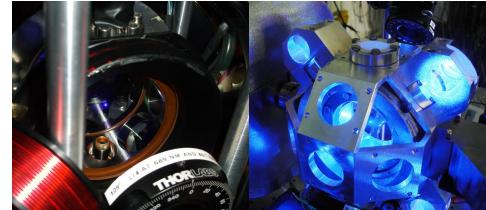
# PERSPECTIVES

- Improved stability and accuracy of OLCs
  - $10^{-19}$  feasible
- Contribution of optical clocks to international timescales
  - redefinition of the SI second
- Extension of the European fiber network for comparison of optical clocks
  - e.g. link between SYRTE and NPL (already established)



# CLOCK ENSEMBLE AT LNE-SYRTE

- 2 Strontium OLCs
  - **J. Lodewyck, R. Le Targat,**  
S. Bilicki, E Bookjans, G. Vallet
- 1 Mercury OLC
  - **S. Bize, L. De Sarlo, M. Favier,**  
R. Tyumenev
- Frequency combs
  - **Y. Lecoq, R. Le Targat,**  
D. Nicolodi
- 3 atomic fountains
  - Cs, Cs/Rb, and Cs (mobile)
  - **J. Guena, P. Rosenbusch,**  
**M. Abgrall, D. Rovera, S. Bize,**  
**P. Laurent**



# FIBER LINK COMPARISON

- LPL

- N. Quintin, F. Wiotte, E. Camisard,  
C. Chardonnet, A. Amy-Klein, O. Lopez



- SYRTE

- C. Shi, F. Stefani, J.-L. Robyr, N. Chiodo,  
P. Delva, F. Meynadier, M. Lours,  
G. Santarelli, P.-E. Pottie



- PTB

- C. Lisdat, G. Grosche, S.M.F. Raupach,  
C. Grebing, A. Al-Masoudi, S. Dörscher,  
S. Hafner, A. Koczwara, S. Koke,  
A. Kuhl, T. Legero, H. Schnatz, U. Sterr



- LUH

- H. Denker, L. Timmen, C. Voigt

