

Constraining the mass of the graviton with the planetary ephemeris INPOP

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arXiv:1901.04307

- ① Massive graviton phenomenology
- ② Numerical analysis
- ③ Results of a global fit

Massive graviton phenomenology

Gravity phenomenology can be derived from particle physics : 2-spin *massless graviton*. Massless or not ?

(Review : C. de Rham, *Massive Gravity*, Living Reviews in Relativity 17, 7 (2014), arXiv:1401.4173)

Different tests of this theory :

- Dispersion relation : $E^2 = p^2c^2 + m_g^2c^4 \Rightarrow$ different waveforms (arXiv:1903.04467)
- Galactic scales (Physics Letters B : 778, 325 – 331 (2018) ; 781, 220 – 226 (2018) ; Annals of Physics 399, 85 – 92 (2018).)
- **Solar system scales : this work.**

Metric tensor in weak field

- In weak field and velocity, almost all massive graviton theories are summarized by a Yukawa potential.
- After expansions in $r/\lambda_g \ll 1$ and clever variable changes :

$$ds^2 = \left(-1 + \frac{2GM}{c^2 r} \left[1 + \frac{1}{2} \frac{r^2}{\lambda_g^2} \right] \right) c^2 dt^2 \\ + \left(1 + \frac{2GM}{c^2 r} \left[1 + \frac{1}{2} \frac{r^2}{\lambda_g^2} \right] \right) d\ell^2$$

$$\lambda_g = \frac{h}{m_g c}, \quad r = \sqrt{x^2 + y^2 + z^2},$$

$$d\ell^2 = dx^2 + dy^2 + dz^2.$$

Geometric optics in massive gravity

Modified time travel :

$$\delta(t_r - t_e) \sim \left(\frac{L}{\lambda_g}\right)^2 \times \text{Shapiro delay}$$

- Previous constrains : $\lambda_g > 10^{12}$ km.
- Solar system scale $\sim 10^9$ km in the worst case (Neptune).

$\Rightarrow \left(\frac{L}{\lambda_g}\right)^2 < 10^{-6}$ for Neptune. Rather $< 10^{-8}$ for solar system bodies with accurate data.

\Rightarrow term negligible, keep usual GR framework.

Planetary dynamics

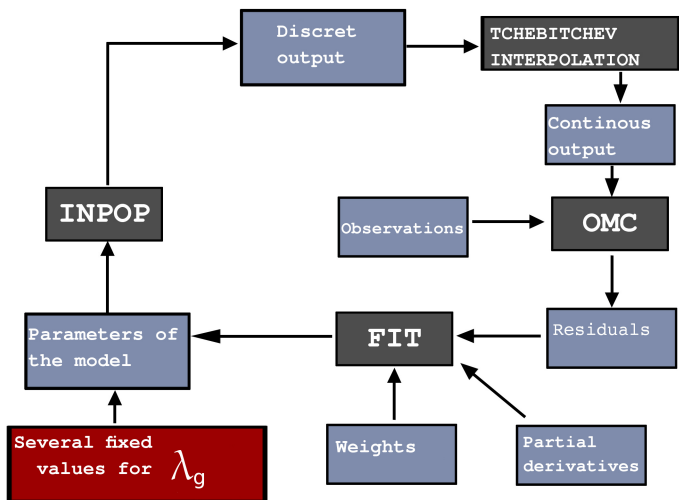
Terms to be added in equations of motion :

$$\delta \frac{d^2 \mathbf{x}_A}{dt^2} = \frac{1}{2\lambda_g^2} \sum_{B \neq A} GM_B \frac{\mathbf{x}_A - \mathbf{x}_B}{|\mathbf{x}_A - \mathbf{x}_B|} + O(\lambda_g^{-3})$$

- Here, $A, B =$ Sun, Mercury, Venus, Earth, Moon, Mars, Jupiter, Saturn, Uranus, Neptune, Pluto.
- Other small bodies: INPOP not changed.
- Clifford Will announced a very good constraint from planetary ephemeris (CQG 35, 17LT01, 2018) :
 $\lambda_g \geq 2.21 \times 10^{14}$ km. 10 times better than LIGO-VIRGO constraints !

Numerical analysis

INPOP and planetary observations



INPOP17b most important
observations

Observations	Time Intervals	#	INPOP17b $\sigma(O - C)$ [m]	INPOP17b-DE436 $\sigma(I - D)$ [m]
Messenger	2011 : 2013.2	950	7.2	3.9
Ody, Mex	2002 : 2016.4	52946	5.0	1.4
Cassini	2004 : 2014	175	32.1	11.7

V. Viswanathan, A. Fienga, M. Gastineau, J. Laskar
2017, INPOP17a planetary ephemerides, scientific notes of IMCCE
<https://www.imcce.fr/inpop/>

INPOP17b = INPOP17a + some extended data from Messenger
(from Verma et al. 2016 Journal of Geophysical Research (Planets)
121, 1627–1640, or arXiv:1608.01360)

- Better are observations and physical model, better are tests of alternative theories.

References :

- V. Viswanathan, A. Fienga, O. Minazzoli, L. Bernus, J. Laskar, M. Gastineau
The new lunar ephemeris INPOP17a and its application to fundamental physics
MNRAS 476, 1877-1888 (2018)
- V. Viswanathan, A. Fienga, M. Gastineau, J. Laskar
2017, INPOP17a planetary ephemerides, scientific notes of IMCCE <https://www.imcce.fr/inpop/>

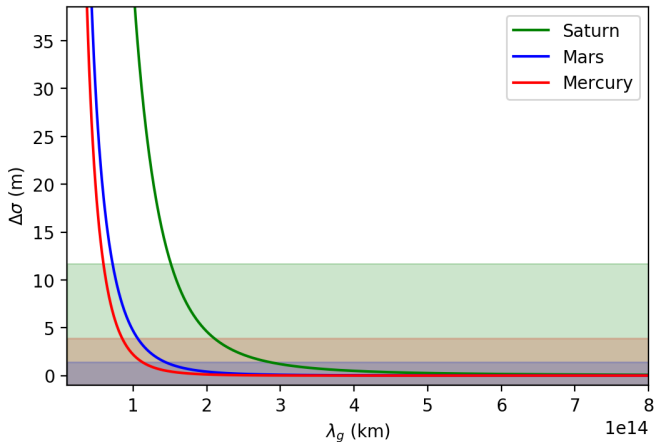
Data analysis

- λ_g fixed, all other parameters are adjusted.
- Same fit for INPOP17b and tested ephemeris (weights, observational data, parameters adjusted).
- After 10 iterations, the fit converges.
- Importance of a global fit : correlations between λ_g and other parameters.

Postfit versus global fit

Postfit

Reference: INPOP17b

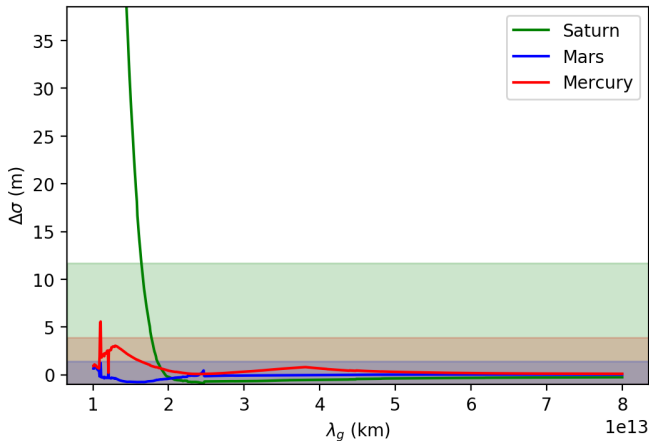


Same order of magnitude as Will's constraint, and seems better than GW constraint! But....

Postfit versus global fit

Global analysis (13 iterations)

Reference: INPOP17b



10 times smaller !

Pearson test for Cassini data

Tests if residuals distribution come from the same distribution function.

From reference residuals distribution, we compute optimal size of bins for modelling histogram.

- $N_i^I =$ hits in bin i for reference solution (INPOP17b)
- $N_i^G(\lambda_g) =$ hits in bin i for tested solution

$$\chi^2(\lambda_g) = \sum_{i=1}^n \frac{(N_i^G(\lambda_g) - N_i^I)^2}{N_i^I}$$

Pearson test for Cassini data

- For Cassini : 175 points \Rightarrow optimal number of bins = 10.
- $\chi^2(\lambda)$ follows a 10 degrees of freedom chi square law.
- Exclusion criterion : for a given value of χ^2 , residuals come from different distribution with a probability p .

$$p = 90\% \quad \Rightarrow \quad \chi^2 \geq 15.99$$

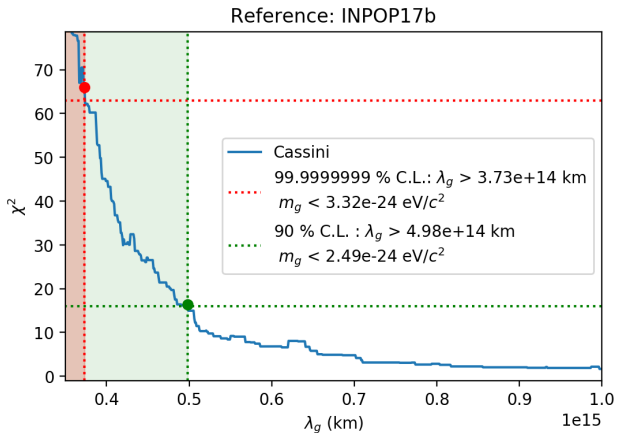
$$p = 99.9999999\% \quad \Rightarrow \quad \chi^2 \geq 62.94$$

Pearson test with postfit analysis

Massive
graviton
phe-
nomenology

Numerical
analysis

Results of a
global fit

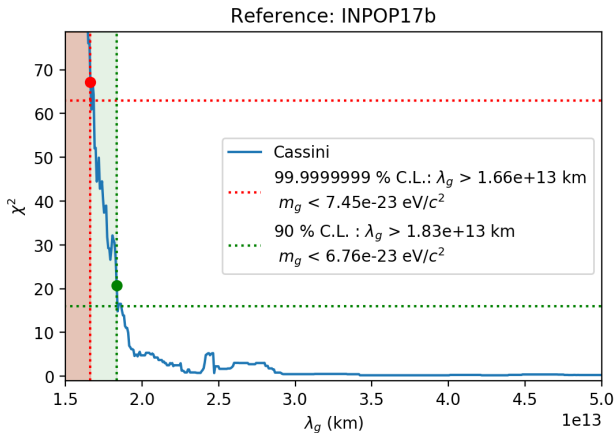


Pearson test with global analysis

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Conclusion

- **For testing a new theory, global fit is crucial!**
- INPOP is a good tool for testing GR in Solar System

Result :

- 90% bound :
 - $\lambda_g > 1.83 \times 10^{13}$ km
 - $m_g < 6.76 \times 10^{-23}$ eV/ c^2
- 99.9999999% bound :
 - $\lambda_g > 1.66 \times 10^{13}$ km
 - $m_g < 7.45 \times 10^{-23}$ eV/ c^2
- Details: arXiv:1901.04307

Future perspectives, work in progress :

- Better constraint criterion based on orbit propagation
- More data and more accurate solution \Rightarrow better constraint.